

# Electron cloud instability in Super B factories and ILC damping ring

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Jan 19, 2009

# Threshold of the strong head-tail instability (Balance of growth and Landau damping)

- Stability condition for  $\omega_e \sigma_z / c > 1$

$$\omega_e = \sqrt{\frac{\lambda_p r_e c^2}{\sigma_y (\sigma_x + \sigma_y)}}$$

$$U = \frac{\sqrt{3} \lambda_p r_0 \beta}{v_s \gamma \omega_e \sigma_z / c} \frac{|Z_{\perp}(\omega_e)|}{Z_0} = \frac{\sqrt{3} \lambda_p r_0 \beta}{v_s \gamma \omega_e \sigma_z / c} \frac{KQ}{4\pi} \frac{\lambda_e}{\lambda_p} \frac{L}{\sigma_y (\sigma_x + \sigma_y)} = 1$$

- Since  $\rho_e = \lambda_e / 2\pi \sigma_x \sigma_y$ ,

$$\rho_{e,th} = \frac{2\gamma v_s \omega_e \sigma_z / c}{\sqrt{3} KQ r_0 \beta L}$$

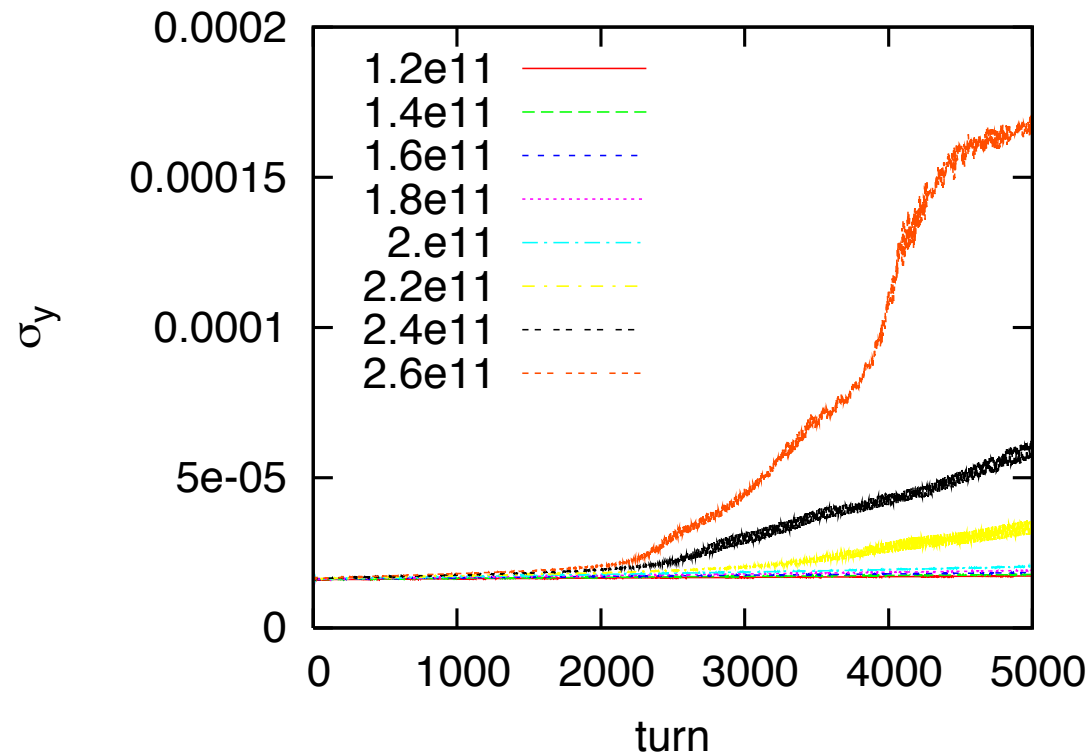
Origin of Landau damping is momentum compaction

$$v_s \sigma_z = \alpha \sigma_{\delta} L$$

- $Q = \min(Q_{nl}, \omega_e \sigma_z / c)$   
 $Q_{nl} = 5-10?$ , depending on the nonlinear interaction.
- $K$  characterizes cloud size effect and pinching.
- $\omega_e \sigma_z / c \sim 12-15$  for damping rings.
- We use  $K = \omega_e \sigma_z / c$  and  $Q_{nl} = 7$  for analytical estimation.

# Threshold of the single bunch instability

- $\rho_{e,th} = 1-2 \times 10^{11} \text{ m}^{-3}$  for Super B factories and ILC damping ring.



# Cloud density estimation

- The cloud density is measured in each element. The integrated (averaged) density can be suppressed to to  $0.5-2 \times 10^{11} \text{ m}^{-3}$  (Suetsugu) for Super B factories.

- ILC damping ring is similar as the Super B factories. Operating current of B factories is higher than ILC damping ring.
- If Super B factories work well, ILC damping ring is no problem for electron cloud instability.